

# **Stochastic modeling of aging cells reveals how damage accumulation, repair, and cell-division asymmetry affect clonal senescence and population fitness**

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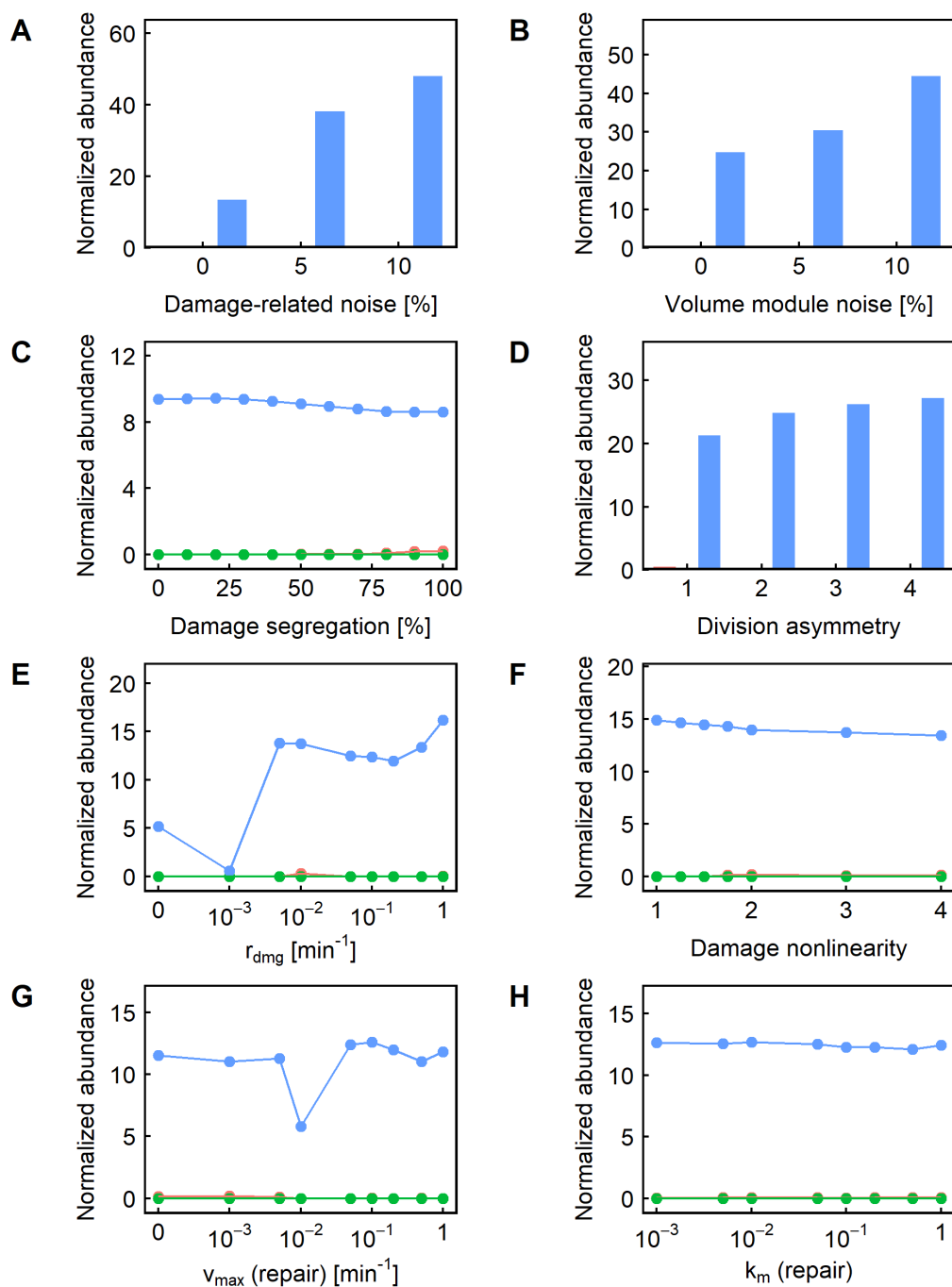
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## **SUPPLEMENTARY INFORMATION**

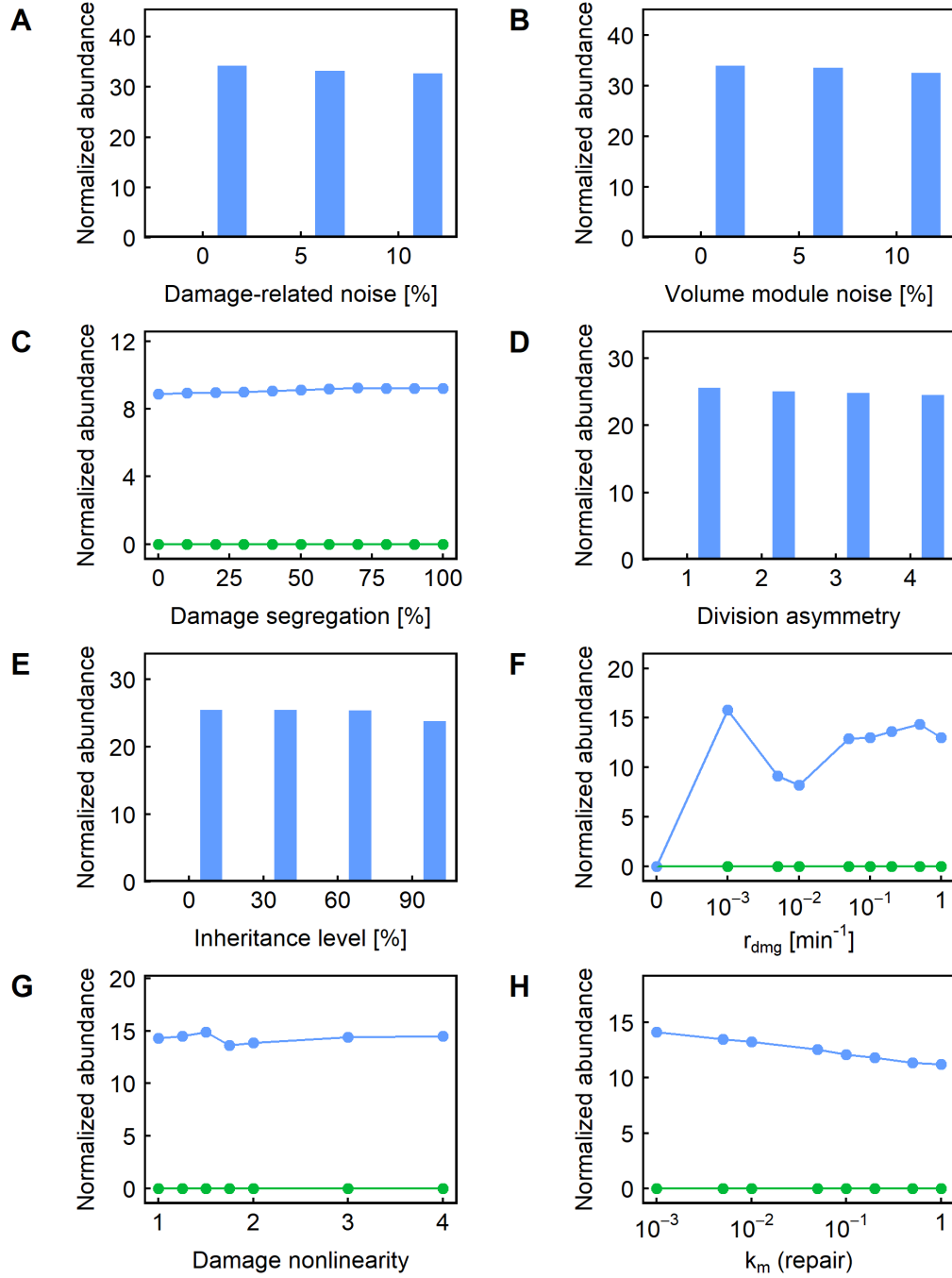
**Supplementary Figures S1-S4**

**Supplementary Tables S1-S2**

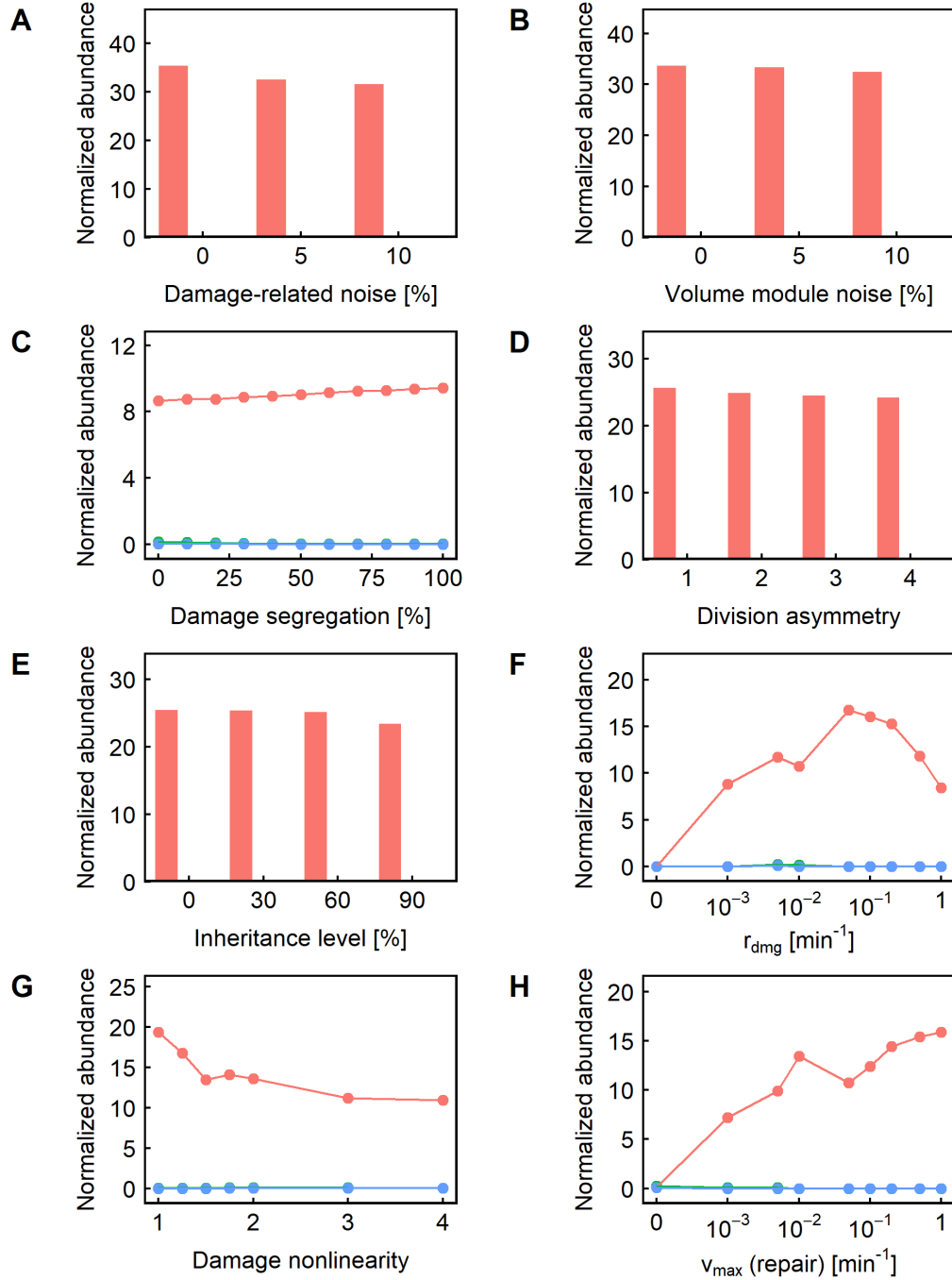
## SUPPLEMENTARY FIGURES



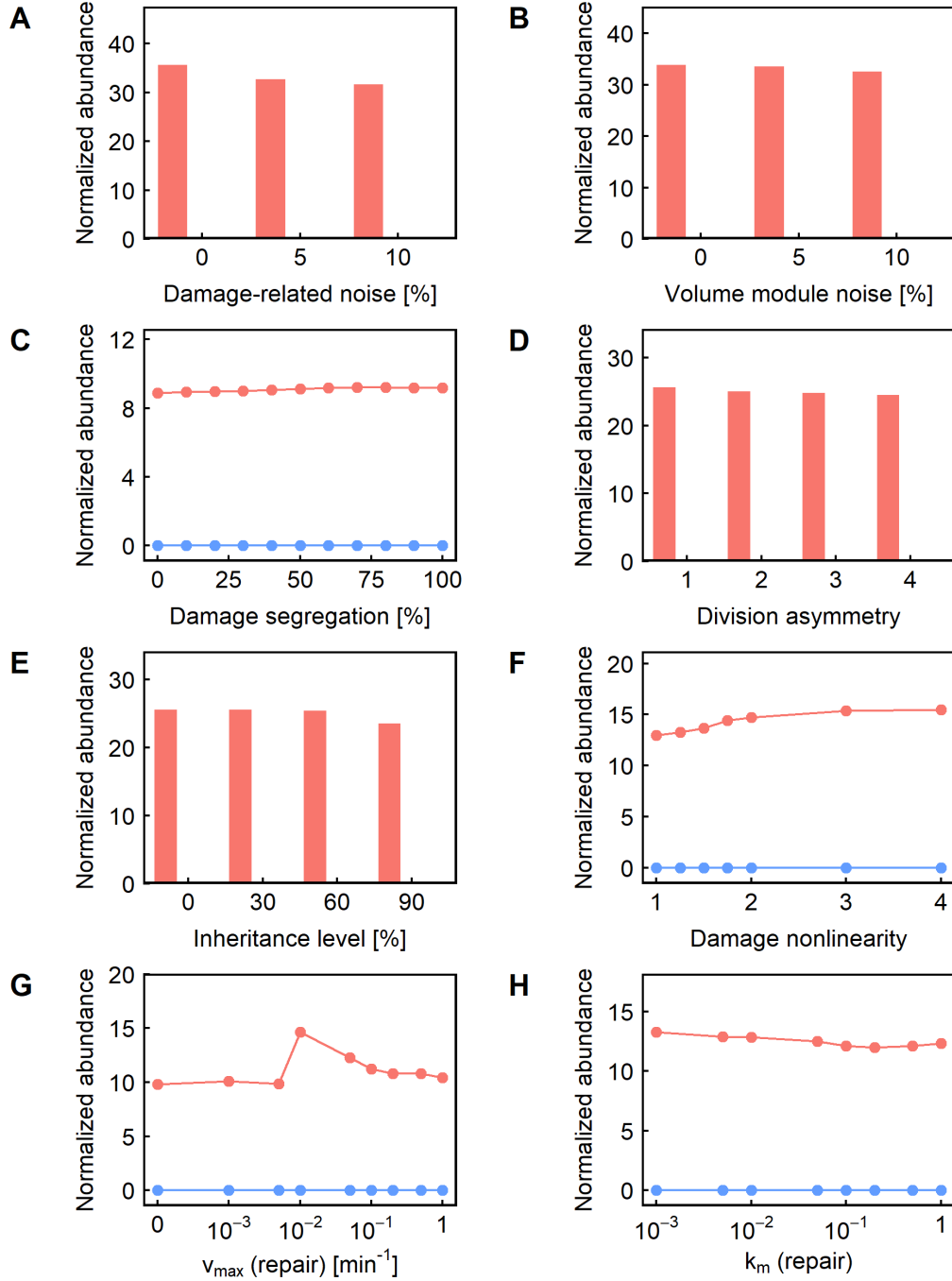
**Fig. S1. A-H.** Relative representation of the other parameters in the cases where changing the level of inheritance caused a significant (>5%) fitness difference. In each panel, the color indicates the level of inheritance resulting in maximum fitness: red indicates that no inheritance ( $c = 0\%$ ) is the most fit; blue indicates that maximum inheritance ( $c = 90\%$ ) is the most fit; and green indicates that an intermediate level of inheritance is the most fit.



**Fig. S2. A-H.** Relative representation of the other parameters in the cases where changing the maximum repair rate caused a significant ( $>5\%$ ) fitness difference. In each panel, the color indicates the level of repair resulting in maximum fitness: red indicates that no repair is the most fit; blue indicates that maximum repair ( $v_{\text{max}} = 1 \text{ min}^{-1}$ ) is the most fit; and green indicates that an intermediate rate of repair is the most fit.



**Fig. S3. A-H.** Relative representation of the other parameters in the cases where changing the Michaelis constant  $k_m$  for repair caused a significant ( $>5\%$ ) fitness difference. In each panel, the color indicates the value of  $k_m$  resulting in maximum fitness: red indicates that the minimum value  $k_m = 0.001$  is the most fit; blue indicates that maximum  $k_m$  ( $k_m = 1$ ) is the most fit; and green indicates that an intermediate value of  $k_m$  is the most fit.



**Fig. S4. A-H.** Relative representation of the other parameters in the cases where changing the damage accumulation rate caused a significant ( $>5\%$ ) fitness difference. In each panel, the color indicates the damage accumulation rate resulting in maximum fitness: red indicates that no damage accumulation is the most fit; blue indicates that maximum damage accumulation ( $r_{\text{dmg}} = 1 \text{ min}^{-1}$ ) is the most fit; and green indicates that an intermediate rate of damage accumulation is the most fit.

## SUPPLEMENTARY TABLES

Parameter	Meaning	Value	Unit
$r_{growth}$	Volume growth rate constant	0.0072	$\text{min}^{-1}$
$V_i$	Initial volume	50	fL
$V_{crit}$	Critical volume (as function of generation $g$ )	$106.7 + 4.628g$	fL

**Table S1. Parameters with fixed mean values.**

Parameter	Meaning	Values	Unit
$c$	Level of inheritance of parameter values	0, 30, 60, 90	%
$R$	Mother/daughter volume ratio at division	1, 2, 3, 4	
$n_d$	Damage-related noise	0, 5, 10	%
$n_v$	Volume module noise	0, 5, 10	%
$s$	Level of damage segregation	0, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100	%
$v_{max}$	Maximum rate of repair	0, 0.001, 0.005, 0.01, 0.05, 0.1, 0.2, 0.5, 1	$\text{min}^{-1}$
$k_m$	Michelis constant for repair	0.001, 0.005, 0.01, 0.05, 0.1, 0.2, 0.5, 1	
$r_{dmg}$	Rate of damage accumulation	0, 0.001, 0.005, 0.01, 0.05, 0.1, 0.2, 0.5, 1	$\text{min}^{-1}$
$\alpha$	Nonlinearity of the effect of damage on growth rate	1, 1.25, 1.5, 1.75, 2, 3, 4	

**Table S2. Parameters with values selected from a grid of values.**